Robust trajectory tracking with non-singular terminal sliding mode control of a mobile manipulator

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ABSTRACT
This effort addresses and uses a robust-trajectory-tracking control system for kinematically redundant location tracking of a mobile manipulator (mobman) in its task space in the presence of parameter uncertainties and external disturbances. It consists of a serial manipulator with four degrees of freedom (DOF) fixed on three DOF mobile bases. A robust tracking control is achieved using the configuration of a non-singular terminal sliding mode (NSTSM) control for the entire non-linear model of a mobman. Because of the non-linear added term in the linear sliding surface, which reflects in the non-linear sliding mode known as terminal sliding mode (TSM), this control preparation satisfies systems states finite time convergence. Similarly, conventional terminal sliding mode control (CTSMC) entail singularity trouble, which is tackled by the control scheme. (Computer based) simulations are used to demonstrate the convenience, feasibility, and robustness of given techniques.

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1. INTRODUCTION
To optimize the robot’s reliable and fast-tracking execution, robust quick tolerant-adaptive-control has been planned. It brings a maximum degree of strength, a quick transitory response, and a finite time convergence method [1]. For a given tracking control scheme, a back stepping control tactic is settled to elude singularity-point matter [2]. Trendy master-slave configuration for a group of mobile robots, path planning based on artificial potential field (APF) united with tracking control mechanism based on FAGNTSMC here [3] the authors have submitted. The authors have suggested an adaptive-fast and stable control way to control robotic manipulator with n-degrees of freedom n-(DOF) [4]. In presence of uncertainties, the non-singular terminal sliding mode control (TSMC) is proposed plus applied to a non-linear four-linked selective compliant assembly robot arm (SCARA) robot-manipulator [5]. Mobile-manipulators have been employed effectively to perform not only effective but also interactive practical assignments like drilling operations and laser cutting, choose an object relocation plus complex surface painting or arc welding, peg-hole addition, and over a long time [6]. Collision avoidance compliance and matter of singularity is defined using an external forfeit utility tactic, domino effect in bounded plus continuous control of mobman even near disturbance limits. Using random profile technique, control the movement of the mobile-manipulator so as to complete a task of pick up.
Which is caused by the mobman’s high mobility plus huge workspace area as compared to a fixed base manipulator. By operating in their task space a mobile-manipulator, they can achieve performance stability, high accuracy, and communicative actions. The core partial of initiate a control is to transfer mobman starting its initial arbitrary place towards aimed position of end effector stated plus great accurateness in chore province coordinates [7]. So far, progress of control algorithms for good tracking enactment is thought-provoking chore on account of dynamic-model of mobman with indeterminate state. Essentially consisting state disparity constraints enforced on mobman crusade and basic uncertain self-motivated equation [8], [9]. Physical uncertainty started by anonymous payload captured by end effector in spite of the fact that the state inequality confinements began in workspace because of the nearness of anonymous issues. The deliberate parametric uncertainties lie in self-motivated conditions and kinematic of mobile-manipulator. Besides, the mobile controller possesses mobile platforms and strong-coupled elements of the controller. So, the plan of the control system turns an inquisitive subject of current investigation for such sorts of uncertain system. For the moment, researchers have turn up for mobile-manipulators tracking control with control procedures as specified in the literature. Including robust adaptive fault tolerant control, chore-null space decoupling control [10], non-linear closed loop control [11], computed torque control (CTC) [12], neural network (NN) [13–15], as a result of complex computation low response time of fuzzy logic control, fuzzy plus NN [16], [17], tracking control that is adaptable and robust, and using a variety of sliding-mode controls [18]. The above study works proposed a self-motivated control law that combines many control procedures such as back stepping, sliding mode, neural-network plus fuzzy logic, making controller design extra laborious, and expensive computationally. Additionally, controllers beginning [19]. Certain controllers in addition to pseudo-inverse [20] require Jacobian-matrix inverse each, within a singular region it may domino effect in mathematical variability. Via Jacobian pseudo inverse general-algorithm specified trend autogenously space pattern matter of inverse-kinematic can be solved [21]. In the middle of above-mentioned control approaches, sliding mode control (SMC) comprise of terminal sliding mode (TSM), and conventional sliding-mode (CSM). In addition to CSM, TSM is finite time stable plus asymptotically stable [22]. Continuous SMC might ensure asymptotic stability mode, implying that the system states will converge to the equilibrium point over a finite settling time. TSM is a non-linear, also planned as per concept of terminal attractor in order to endorse finite time convergence [23], [24]. TSM, compared with traditional SMC, provides quick besides finite time convergence, making it ideal for high-precision control. Singularity is an issue with TSM controller design procedures. A major reading has been done towards ignoring trouble of singularity via non singular terminal sliding mode power control (NTSMC) [25]. SMC is designed in both stages: the first is to elect a sliding-mode surface, and next to design a SMC to ensure sliding mode presence and drive mechanism to acquire switching manifold in a finite amount of time plus stay there. Now, NTSMC based trajectory tracking control design is presented then used for a mobman complete model (non-linear). This dynamical model of a mobile-manipulator incorporates outer quandaries such as parameter uncertainties, noises, and the sensor used for measurement. The foremost contributions of article are stated is being as: a robust trajectory tracking control law of a ... (Shankar J. Gambhire)
mobman links angles too joint-displacement of manipulator each. The $f_{\text{dis}}$ is vector of lumped disturbance which holds system uncertainties, frictional effects and peripheral difficulties, vector of manipulator moments plus inertial forces: $M(q)\ddot{q}$, centripetal and coriolis vector effects for manipulator: $C(q, \dot{q})\dot{q}$, vector due to manipulator’s gravity-effects: $g(q)$ control-input torques vector: $\tau = [\tau_m, \tau_b]^T \in \mathbb{R}^{7 \times 1}$, wherever, input torques vector: $\tau_m \in \mathbb{R}^{4 \times 1}$ unstated for serial-manipulator control fixed on mobman plus $\tau_b \in \mathbb{R}^{3 \times 1}$: input-torque vectors towards control mobile-manipulator base. ($f_{\text{dis}}$): vector of lumped trouble agreed as:

$$f_{\text{dis}} = f_{\text{edis}} + f_{\text{idis}}$$  \hspace{1cm} (2)

where, $f_{\text{edis}}$: vector of external-disturbances acting on mobile-manipulator,$f_{\text{idis}}$: internal disturbances vector despite parametric disturbances besides uncertainties caused as a result of measurement noises and may be given as:

$$f_{\text{idis}} = \Delta M(q)\ddot{q} + \Delta (C(q, \dot{q}))\dot{q} + \Delta g(q) + F(q, \dot{q})\dot{q} + \nu$$  \hspace{1cm} (3)

Figure 1. Planned mobman conceptual design

Table 1. Mobman structure specifications

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>over-all weight of base</td>
<td>15 kg</td>
</tr>
<tr>
<td>over-all height</td>
<td>300 mm</td>
</tr>
<tr>
<td>diameter with circular base</td>
<td>500 mm</td>
</tr>
<tr>
<td>Mobile base Allowable payload</td>
<td>12 Kg</td>
</tr>
<tr>
<td>Maximum base velocity</td>
<td>0.8 meter/sec</td>
</tr>
<tr>
<td>Type</td>
<td>Omni Directional</td>
</tr>
<tr>
<td>No. of helms</td>
<td>4 (singly driven)</td>
</tr>
<tr>
<td>Diameter</td>
<td>47.5 mm</td>
</tr>
<tr>
<td>No. of axix</td>
<td>4 (PRRR configuration)</td>
</tr>
<tr>
<td>Height</td>
<td>1.000 mm (trendy extended mode)</td>
</tr>
<tr>
<td>Reach</td>
<td>500 mm (trendy extended mode)</td>
</tr>
<tr>
<td>Work Envelope</td>
<td>0.625 m 3</td>
</tr>
<tr>
<td>Payload</td>
<td>2 Kg</td>
</tr>
<tr>
<td>Axis speed</td>
<td>90 deg/sec</td>
</tr>
<tr>
<td>Manipulation link (ML) 1: Length</td>
<td>300 mm</td>
</tr>
<tr>
<td>ML 2: length</td>
<td>200 mm</td>
</tr>
<tr>
<td>Maximum Limit of Prismatic Joints</td>
<td>500 mm</td>
</tr>
<tr>
<td>ML: 1 mass</td>
<td>5 kg</td>
</tr>
<tr>
<td>ML: 2 mass</td>
<td>3kg</td>
</tr>
<tr>
<td>Actuators</td>
<td>BLDC motors (24 VDC) with 75 W drive train power limit</td>
</tr>
</tbody>
</table>

where $\Delta (M(q))\ddot{q}$, $\Delta (C(q, \dot{q}))\dot{q}$, and $\Delta g(q)$ remain signal-uncertainties in $M(q)\ddot{q}$, $C(q, \dot{q})\dot{q}$, and $g(q)$ each one. $F(q, \dot{q})\dot{q}$ vector represents frictional effects (static, coulomb, and viscous) due to joint of manipulator. Vector”$\nu$” appears inside disturbances presented by position velocity estimation devices. For framework flow,
earth-fixed vector representation believed through properties of a mobile-controller system. Specified below
are finite dimensional.

Property 1. Positive symmetric and definite (PDS) is inertia matrix $M(q)$.

$$M(q) = M^T(q) > 0, \forall q \in \mathbb{R} \quad (4)$$

Property 2. In addition to $m_m$ non-negative constants take place $m_M$ i.e. $m_M \leq \| M(q) \| \leq m_M$.
The matrix $M(q) - 2C(q, \dot{q})$ is a skew symmetric matrix i.e.

$$s^T[M(q) - 2C(q, \dot{q})]s = 0, \forall s \in \mathbb{R}, q \in \mathbb{R} \quad (5)$$

2.2. Control system design

By way of forcing the states $q$ for tracking the desired-position $q_d$ is the objective of this control. Definition of tracking error can be given as,

$$e = q_d - q \quad (6)$$

where, desired trajectory is $q_d$. As per (1) designation of a terminal siding surface (non-singular).

$$s(t) = e(t) + \frac{1}{p} \dot{e}(t) = 0. \quad (7)$$

Where $\beta = \text{diag}[\beta_1, \cdots, \beta_i, \cdots, \beta_n]$ in which a positive constant is $\beta_i$, $p$ and $q$ are non-negative odd integers , which satisfy the situation as given as:

$$p > q. \quad (8)$$

Condition for sufficiency to demonstrate existence of TSM equally:

$$\frac{1}{2} \frac{d}{dt}s_i(t)^2 < -\zeta_i \left| s_i(t) \right| \quad (9)$$

where positive constant is $\zeta_i (i = 1, \cdots, n)$. TSM is mentioned in (1): $s_n(t) = 0$ its dynamics utilising non-linear differential equation gained:

$$-\dot{e}(t)^\frac{q}{p} = e(t)\beta \quad (10)$$

Infinite period of time with $e(t)$ approach terminal-sliding surface $t_{ri} (i = 1, \cdots, n)$, as $s(t) \neq 0$, which fulfills:

$$t_{ri} \leq \frac{\left| s_i(0) \right|}{\zeta_i} \quad (11)$$

Mobman structure is stable when NTSMC control law chosen in place of supposing NTSMC, sufficient condition given in (7) and (9):

$$\tau = \left( \ddot{q}_d + \frac{\beta q}{p} \dot{e}(t)^{2-\frac{q}{p}} + \zeta \text{sgn}(s) \right) M(q) + C(q, \dot{q})\dot{q} + g(q)$$

$s\text{gn}(s)$ discontinuous function (Df) as per above equation chattering of control-input will be provided. Chatter is a detrimental phenomenon as it leads to decrease control accuracy, moving mechanical parts matrix high wear too power circuits with high heat losses. Exploitation of digital controllers with finite sampling rate is chattering, also called ‘discretization- chatter’. Ideally best sliding mode hint at infinite switching frequency. Subsequently within a sampling interval control is constant, switching frequency cannot exceed that of sampling, which lead to chattering as well increases the energy consumption of the controller. This Df $sgn(s)$ replaced through continuous $\text{sat}(s, \Phi)$ called saturation-function, to compensate undesirable control chattering, can be defined: where, boundary layer thickness is $\Phi_i$.

$$\left\{ \text{sat}(s, \Phi) \right\}_i = \begin{cases} \frac{s_n_i}{\Phi_i} & \text{if } s_n_i > \Phi_i \\ \frac{s_n_i}{\Phi_i} & \text{if } s_n_i \leq \Phi_i \end{cases} \quad (12)$$

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2.3. Stability analysis

Now, ‘Lyapunov-stability analysis’ way is useful to reveal convergence property of offered NTSMC controller. Assumptions made to elucidate stability-analysis of given NTSMC controller, could be as shown in.

Assumption 1. Term well-known as $ f \text{dis} $ lumped disturbance is bounded, be made up of constant $ 0 \leq | f \text{dis} | \leq F_{\text{max}} $.

Assumption 2. $ \dot{q} $ and $ q $ states are available to measure the quantity which is to be measured.

Assumption 3. $ q_d $ required trajectory is smooth along with double-differential i.e. $ q_{dd}, \dot{q}_{dd}, \ddot{q}_{dd} $ too reachable by means of well-identified boundaries.

2.3.1. Theorem

Take up both properties with mobile-manipulator dynamics (1). Vector of control input is taken as defined (12). Error vector monitoring output touches to zero in an infinite amount of time with respect to $ s $.

2.3.2. Proof

Take up Lyapunov-candidate function recognised for instance, $ V = \frac{1}{2} Ms^T s $ (13)

Taking derivative of $ V $ from (13), it becomes,

$$ \dot{V} = \frac{1}{2} \left\{ s^T Ms + s^T \dot{M}s + s^T M\dot{s} \right\} $$

Since $ s^T M\dot{s} = s^T M s, \dot{M} = 2C(q, \dot{q}) $ (property 2) can be solved as,

$$ \dot{V} = s^T \left\{ M \dot{s} + C(q, \dot{q})s \right\} $$

$$ \dot{V} = s^T \left\{ M \left( \dot{e}(t) + \frac{1}{\beta q} \text{dia}(\dot{e}(t)^{\frac{q}{p}} - 1)\ddot{e}(t) \right) + C(q, \dot{q})s \right\} $$

$$ \ddot{e}(t) = \dot{\eta}_d - \dot{\eta} $$

As mentioned in (1) and (12), it gives,

$$ \ddot{e}(t) = -\frac{q}{p} \beta (\text{dia}(\dot{e}(t)^{2 - \frac{q}{p}})) - \zeta sgn(s) - M^{-1} f \text{dis} $$

Putting value of $ \ddot{e}(t) $ to (16) through (18) it becomes,

$$ \dot{V} \leq s^T \left\{ \frac{1}{\beta q} \text{dia}(\dot{e}(t)^{\frac{q}{p}} - 1) \left[-M \zeta \text{sgn}(s) - f \text{dis} \right] \right\} + s^T C(q, \dot{q})^T s $$

1 < $ \frac{q}{p} $ < 2 as $ p $ and $ q $ are positive odd integers, there is $ \dot{e}(t)^{\frac{q}{p}} - 1 > 0 $ so, negative definite would be Lyapunov-function (V) time-derivative if and $ V $ fulfils differential inequality as per (20) as shown in (21),

$$ | \zeta_i | \geq | \tau_{\text{dis}} | $$

$$ \dot{V}(t) \leq V(t)^\alpha (-\gamma) $$

It consists, $ \alpha \in (0, 1) $ plus $ \gamma > 0 $. In (22), the parameters $ \alpha $ and $ \gamma $ are defined such that to have (22) as negative definite and hence stable. Here, the value of $ \gamma $ has to be positive constant to ensure negative definiteness of (22) and hence considered as $ \gamma_i > 0 $. To have convergence of V with respect time towards zero, the value of parameter $ \alpha $ has to be selected between 0 and 1. Hereafter, as per Lyapunov-stability standards converges to zero infinite time a non-linear plus non-singular sliding surface given in (7).
3. RESULTS AND DISCUSSION

3.1. Description of planned structure

In-depth computer-based simulations were conducted to demonstrate potential of control strategy on offered robotic framework. Given controller framework comprise of 4 DOF (PRRR) mounted on 3 DOF mobile-base of serial controller. Test-case is picked so that manipulator begins on starting point, reaching-back to the initial point afterwards roving a given multipart set way. During activity, the controller selected uncertain mass body and positioned it in a specific location (i.e. 2 KG pay-load engaged into thought for recreation), transmit mass of load (un-identified) along the aforementioned foreordained way in addition put the question at focused on point of the area.R) mounted on 3 DOF mobile-base of serial controller.

3.2. Performance analysis

This sub-division, Figures 2-5 denotes computer-based simulation outputs for chore space trajectory revealed overhead. Deviation in payload is from 0 kg to 2.5 kg (no load to payload full). In addition, structure uncertainty differs (-40% to 40%), controller robustness has been specialized to get a suitable considerate of scheme robustness, over and above scheme uncertainty vector of external-disturbance is included, and is presented is being as,

$$\delta_{\text{dis}} = \begin{bmatrix} 5 \cos(w_d t) \\ 5 \sin(w_d t) \\ 5 \cos(w_d t) \end{bmatrix} \text{ in } \text{N}$$ \hspace{1cm} (22)

Where, external disturbance frequency is $w_d$, brings out simulations to find performance of controller in case of speedy disturbance change and changes (0-2 rad/s. Comparative study has been supported to appear the legitimacy of the proposed strategy, with renowned controllers alike linear proportional+integral+derivative (PID) CTC. For mentioned controllers control laws can be expressed as:

$$\eta = K_P \ddot{q} + K_I \int \dot{q} dt + K_D \frac{d\ddot{q}}{dt} : \text{PID}$$

$$\eta = \dot{M}(q)(\ddot{q} + K_1 \dot{q} + K_2 \dot{q}) + \dot{C}(q, \dot{q}) \ddot{q} + \ddot{g}(q) : \text{CTC}$$

To achieve a better comparison, the following errors and controller gain matrices are set to be about the same to facilitate altogether controllers agreeable control execution under archetypal situations. (i.e. $f_{\text{dis}} = 0$). Controller LPID variables: $K_P = 6.5$, $K_I = 3.5$, $K_D = 1.25$; for CTC, $K_1 = 4.56$, $K_2 = 6.32$. In lieu of suggested NTSMC: $q = 3$, $\beta = 8$, $p = 5$, $\zeta = 15$, and $\Phi = 0.009$. The three-dimensionless view of tracking responses given by all the control methods have been shown in Figure 2. It can be clearly seen that proposed controller shows better tracking performance compared with PID and CTC methods. For complex-chore space position-controllers relational result the following control at the side uncertain condition as appeared in Figure 3. It may say that controller viably takes after desired multipart route also brings out moving object at same time, as per result. The CTC and LPID ways offer significant inaccuracies with trajectory following, inadequately in overseeing external-disturbances plus parameter-uncertainties. Noticing chore-space time histories inaccuracies set by controllers established plus time trajectories of tracking-error norm (Euclidean-norm) are shown in Figure 4 and justifies the pitched scheme performance. Figure 5 shows the control efforts given by proposed control method. A quantitative analysis of the tracking performance of a mobman given by all the controllers in terms of integral of the absolute error (IAE), root mean square of the error (RMS), and integral of the time absolute error (ITAE) is done and given in Table 2 from which, it is confirmed that as compared to other controllers the proposed control scheme gives minimum tracking errors in x, y, and z directions.

<table>
<thead>
<tr>
<th>Control Schemes</th>
<th>$\mu_x$</th>
<th>$\mu_y$</th>
<th>$\mu_z$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RMS</td>
<td>IAE</td>
<td>ITAE</td>
</tr>
<tr>
<td>LPID</td>
<td>0.0675</td>
<td>55.5897</td>
<td>24839</td>
</tr>
<tr>
<td>CTC</td>
<td>0.0286</td>
<td>21.6217</td>
<td>9371.9</td>
</tr>
<tr>
<td>NTSMC</td>
<td>0.0019</td>
<td>0.3511</td>
<td>78.8374</td>
</tr>
</tbody>
</table>

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Figure 2. Trajectory tracking-control (TTC) with indefinite condition (3D view)

Figure 3. The time history for tracking task space deviations by (a) LPID, (b) CTC, and (c) NTSMC method

Figure 4. Deviances in norm variations of the tracking location all through multipart chore space trajectory-tracking control thru indeterminate condition
4. CONCLUSION

For combined prearranged chore-space motion control of 7-DOF manipulator mode (mobile), a non-singular non-linear robust TSM control algorithm is presented as well as useful. The utility of submitted way has been verified by matching results to that of existing controllers. The proposed performance better in form of tracking, finite time error convergence plus robustness, according to simulation results.

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